ELECTRON TRANSPORT AND SECONDARY EMISSION IN A SURFACE OF SOLAR CELL

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Abstract— We study the primary discharge of a solar cell involving secondary emission and desorption. By establishing a fluid model, numerical simulation are performed leading to qualitative informations with regard to the plasma generated by the discharge.

I. Introduction

Future solar arrays are being designed for much higher voltage operations in order to meet high power demands. During the use of high voltage solar arrays, discharges mostly occur on the surface of the solar cells. According to recent publications, the trigger of electric arcs involves the creation of a primary discharge where electron secondary emission plays an important role.

A schematic of a conventional solar cell is shown in figure 1.

Figure 1 : Conventional solar cell

In a recent work, M.Cho and D.E.Hasting (refs. 4,5) studied the mechanism of secondary arcs formation. They suggested that a neutral gas is desorbed from the side surface of the coverglass by electron bombardement, a phenomenon known as Electron Stimulated Desorption (ESD). The bombarding electrons are emitted from the interconnector, as observed experimentally and determined by Snyder et al (ref 11) and also from the coverglass as a result secondary electron emission. Then the desorbed neutrals accumulate in the gap between the coverglass and the interconnector forming a high pressure gas layer which can breakdown because of the electron current flowing through it.

Figure 2

The model studied by M.Cho and D.E.Hasting (Refs 4,5) is shown on figure 2. It consists in dielectric materials placed on a negatively biased conductor in a plasma environment. For a solar array, the dielectrics materials corresponds to the coverglass and adherives and the conductor corresponds to the interconnector. The solar cell itself is considered lumped with the interconnector.

In this configuration Cho and Hasting (Refs. 4,5) studied the charging of the dielectric materials. They proposed a numerical model for the mechanism of the electric arc formation. The simulation, which are based on particle methods, are stopped when the plasma density becomes too large.

The purpose of this paper is to study the primary discharge and the generated plasma by establishing a fluid model leading to a more macroscopic description than the model given by (Refs. 4,5) and then, enabling numerical simulations at a lower cost. According to M.Cho and D.E.Hasting (Refs 4,5) we suppose that the primary discharge is due to a combination of enhanced field emission at certain sites (particularly, the triple point where metallic parts, dielectrics and vacuum meet), electron secondary emission and electron stimulated desorption of the neutral gas adsorbed on the surface. The important terminologies we use regarding to the region of interest are dielectric side surface, the surface perpendicular to the conductor surface; dielectric front surface, the surface parallel to the conductor; the triple point where the conductor, the dielectric and the vacuum meet; and interconnector region, the region near the triple junction where the electric field is strong (see figure 3).

II. Mathematical modelling

From a kinetic model, P. Degond (Ref. 6) has derived a diffusion model describing the motion of charged particles in a surface potential subject to collisions with a solid surface. In this configuration the electrons emitted from the metallic parts are confined along the dielectric surface and undergo many collisions with the surface (see [12] for more details and references). We consider that particles emitted from the triple point are subject to a longitudinal potential \( \Phi_0 (x) \) which transports them along the dielectric surface. In a same time, particles are attracted back to the surface by a transverse potential \( \Psi (x) \). Particles colliding with the surface suffer a large number of physical process, like attachment to the side surface and secondary emission. For the rigorous derivation of the model, the interaction of the electrons with the side surface should be nearly elastic. In pratice, this is not really the case but the model still leads to satisfactory results (see [12] for more details and references). The resulting macroscopic dynamics of the electrons along the surface is a diffusion process in an extended space consisting of the position and the energy coordinates of the electrons. It consists of a diffusion equation for the distribution function \( F(x, \varepsilon) \). The quantity \( N(\varepsilon) F(\varepsilon) \, d\varepsilon \) is the number of particles in a
volume, \( dx \) near the point \((x, \varepsilon)\). \( N(\varepsilon) \) is the 'density of state' (see Ref. 6) and is given by

\[
N(\varepsilon) = \frac{8\sqrt{2\pi}}{3} \frac{1}{q|E_T| m^{3/2}} \varepsilon^{3/2}
\]

in the case of a linear transverse potential profile

\[
\Psi(z) = -E_T z.
\]

where \( E_T \) is the electric field in the perpendicular direction to the dielectric side surface.

A. The energy transport model

A.1 Derivation of the energy transport model

The model derived in (Ref. 6) gives access to the energy distribution function which is an important quantity but this model remains expensive compared with usual fluid models. Therefore in this section we shall consider the Energy Transport model by assuming that the electrons are in local equilibrium and then the energy distribution function \( F(x, \varepsilon) \) is a Maxwellian distribution

\[
F(x, \varepsilon, t) = F(\varepsilon) = \exp \left( \frac{\mu(x, t) - \varepsilon}{E_T(x, t)} \right)
\]

where \( \mu \in \mathbb{R} \) and \( T_e > 0 \) are parameters respectively called the chemical potential and the temperature of the electrons, which depend on \( x \) and \( t \).

As the phenomena (in particular secondary emission ) take place essentially along the dielectric surface, we will consider a one dimension problem.

Therefore given the interpretation of \( F(x, \varepsilon) \), for the Maxwellian distribution \( F(\varepsilon) \), we define the surfacic density \( n_e \) (m\(^{-2}\)) and the surfacic energy density \( W_e \) (eV m\(^{-2}\)) of the electrons by

\[
\left\{ \begin{array}{l}
n_e(x, t) = \int_0^{+\infty} F(\varepsilon) N(\varepsilon) \, d\varepsilon \\
W_e(x, t) = \int_0^{+\infty} F(\varepsilon) \varepsilon N(\varepsilon) \, d\varepsilon
\end{array} \right.
\]

where we recall that \( N(\varepsilon) \) is the 'density of state'.

In the case of the Maxwellian (3) and of the linear potential profile (2) we have

\[
n_e = C(T) \varepsilon^{5/2} e^{\varepsilon/T_e}, \quad C(T) = C_0 \varepsilon^{5/2} e^{\varepsilon/T_e}, \quad C_0 = \left( \frac{2\pi k}{m_e} \right)^{3/2}
\]

\[
W_e = \frac{5}{2} n_e T_e
\]

Integrating the diffusion model of (Ref. 6) with respect to \( \varepsilon \), we find that \( n_e(x, t) \) and \( W_e(x, t) \) satisfy the following system

\[
\frac{\partial}{\partial t} n_e + \nabla_x j_n = q_n,
\]

\[
\frac{\partial}{\partial t} W_e + \nabla_x j_w - j_n \nabla_x \Phi_0 = q_w,
\]

where

\[
\begin{align*}
\lambda_n &= -D_{11} \left( \frac{\mu}{T} - \frac{\nabla_x \Phi_0}{T} \right) - D_{12} \nabla_x \left( -\frac{1}{T} \right), \\
\lambda_w &= -D_{21} \left( \frac{\mu}{T} - \frac{\nabla_x \Phi_0}{T} \right) - D_{22} \nabla_x \left( -\frac{1}{T} \right)
\end{align*}
\]

\( \lambda_n \) and \( \lambda_w \) being respectively the particle and energy currents; \( \Phi_0 \) is the longitudinal potential along the surface where \( E_0 = -\nabla_x \Phi_0 \) is the electric field in the parallel direction to the dielectric side surface. The longitudinal potential \( \Phi_0 \) is determinated by solving Poisson equation

\[
-\Delta \Phi_0 = \frac{q}{\varepsilon_d} \left( \frac{n_s}{\varepsilon_d} - \frac{n_e}{\varepsilon_0} \right)
\]

where \( n_s \) is the positive surface charge accumulated by electron secondary emission, \( \varepsilon_d \) is the dielectric constant of the dielectric surface, \( \varepsilon_0 \) is the permittivity of free space and \( d \) is the layer of the electron plasma cloud. For the simulation we estimate this layer by the following quantity

\[
d = \frac{T_e}{2 |E_T|}
\]

\( q_s \) and \( q_w \) are terms of relaxation which takes account of the surface inelastic interactions and were be defined in the next section.

The diffusion matrix \( D \) is a symmetric \( 2 \times 2 \) matrix

\[
D = \begin{pmatrix}
D_{11} & D_{12} \\
D_{21} & D_{22}
\end{pmatrix}
\]

and the coefficient \( D_{ij} \) are given by

\[
\begin{align*}
D_{11} &= \frac{D_{11}}{T_e^2} n_e T_e^{3/2}, \\
D_{12} &= \frac{D_{12}}{T_e^2} n_e T_e^{5/2}, \\
D_{22} &= \frac{D_{22}}{T_e^2} n_e T_e^{7/2}, \\
D_0 &= \frac{2}{2} \sqrt{\frac{2\pi}{m_e}}
\end{align*}
\]

where \( m_e \) is the electron mass and \( q \) is the elementary charge

The particle and the energy currents \((8)-(9)\) can be expressed in term of a mobility rate, therefore we have

\[
\begin{align*}
\lambda_n &= \mu_n \left[ n_e \nabla_x \Phi_0 - \nabla_x (n_e T_e) \right] + \alpha \nabla_x T_e \\
\lambda_w &= \mu_w \left[ n_e \nabla_x \Phi_0 - \nabla_x (n_e T_e) \right] - \kappa \nabla_x T_e
\end{align*}
\]

\( \mu_n \) and \( \mu_w \) are respectively the particle and the energy mobilities; \( \alpha \) and \( \kappa \) are respectively the thermoelectric coefficient and the thermal conductivity.

In the case of the linear transverse potential profile (2), these parameters are given by

\[
\begin{align*}
\mu_n &= \frac{D_{11}}{n_e T_e}, \\
\mu_w &= \frac{D_{12}}{n_e T_e}, \\
\alpha &= \frac{D_{11}}{n_e T_e} \left( \frac{C(T_e)}{C(T)} + 1 \right) - \frac{D_{12}}{T_e^2}, \\
\kappa &= -\frac{D_{12}}{n_e T_e} \left( \frac{C(T_e)}{C(T)} + 1 \right) + \frac{D_{22}}{T_e^2}
\end{align*}
\]

A.2 The entropic structure of the energy-Transport system

It is more convenient to introduce the following variables

\[
\varepsilon_F = \mu - \Phi_0; \quad W_{\varepsilon T} = W_e - n_e \Phi_0; \quad j_{\varepsilon T} = j_w - j_n \Phi_0
\]
where $\varepsilon_F$ is the Fermi energy or electro-chemical potential, $W_{eT}$ is the total energy and $j_w$, is the total energy current. Then the Energy-Transport model system (ref) can be written as

$$\frac{\partial}{\partial t}m_e + \nabla_x j_n = q_n,$$  
(17)

$$\frac{\partial}{\partial t}W_{eT} + n_e \frac{\partial \Phi_0}{\partial t} + \nabla_x j_w = q_w - q_n \Phi_0,$$  
(18)

with

$$j_n = -\tilde{D}_{11} \left( \nabla_x \left( \frac{\varepsilon_F}{T} \right) \right) - \tilde{D}_{12} \nabla_x \left( -\frac{1}{T} \right),$$  
(19)

$$j_w = -\tilde{D}_{21} \left( \nabla_x \left( \frac{\varepsilon_F}{T} \right) \right) - \tilde{D}_{22} \nabla_x \left( -\frac{1}{T} \right)$$  
(20)

and

$$\tilde{D}_{11} = D_{11}, \quad \tilde{D}_{12} = \tilde{D}_{21} = D_{12} - \Phi_0 D_{11} \quad \text{and}$$  
$$\tilde{D}_{22} = D_{22} - 2\Phi_0 D_{12} + \Phi_0^2 D_{11}.$$  
(21)

### III. Surface inelastic interaction

The electron surface interactions involve inelastic mechanisms such as attachment, secondary emission and desorption of adsorbed neutral. In addition the electrons can suffer collision with free neutral molecules present in the vacuum. In this section, we shall only discuss surface inelastic collisions and we neglect collisions with atoms and leave it for future work.

#### A. Electron secondary emission

In the energy transport system (17), (18), the two terms $q_n$ and $q_w$ are defined by

$$q_n = q_n^+ - q_n^-, \quad (22)$$

$$q_w = q_w^+ - q_w^-, \quad (23)$$

the loss terms (with a minus exponent) corresponding to the attachment on the dielectric side surface and the gain term (with a plus exponent) corresponding to a reemission.

The loss term can be written in the case of a linear transverse potential profile by

$$q_n^- = \nu_0 n_e W_e,$$  
(24)

$$q_w^- = \frac{4}{5} \nu_0 W_e,$$

where $\nu_0$ is a collision frequency with the dielectric side surface given by

$$\nu_0 = \sqrt{\frac{q}{2\pi m_e}} \frac{|E_r|}{T_e} \quad \text{s}^{-1} \quad (25)$$

The ‘yield’ $\gamma_{es}$ for the creation of secondary electrons is strongly dependent on the energy and angular distribution of the incident electrons. The following formula, given by (Ref. 4), for $\gamma_{es}$ is used

$$\gamma_{es} = \gamma \left( \varepsilon, \theta \right) = \gamma_{max} \frac{E_{max}}{\varepsilon \varepsilon_T} \exp \left( 2 - 2 \sqrt{\frac{E_{max}}{\varepsilon}} \exp \left( 2 \left( 1 - \cos \left( \theta \right) \right) \right) \right) \quad (26)$$

where $\varepsilon$ is the incident energy, $E_{max}$ is the incident energy for the maximum secondary electron yield, $\theta$ is the incident angle and $\gamma_{max}$ is the maximum secondary yield at normal incidence.

We assume an isotropic distribution of the incident electronic particles and we define the mean yield (number of electrons reemitted for given incident energy $\varepsilon_i$) by

$$g \left( \varepsilon' \right) = \frac{\gamma_{max}}{E_{max}} \exp \left( \frac{2}{2} \exp \left( 2 - 2 \sqrt{\frac{E_{max}}{\varepsilon_i}} \right) \right) \left( -2 \sqrt{\frac{E_{max}}{\varepsilon_i}} \right) \quad (27)$$

In order to define a physical model of secondary emission the following assumptions are made for one given incident electron:

- the incident electron is reemitted with 90% of its incident energy.
- secondary electrons are emitted and share uniformly the 10% remaining energy.

With these assumptions the gain term due to secondary emission are given by

$$q_w^+ = \nu_0 n_e W_e \quad (28)$$

$$q_w^- = \frac{4}{5} \nu_0 W_e \quad (29)$$

#### B. Electronic stimulated desorption

In this section, we are interested in the neutral density generated by Electron Stimulated Desorption. Indeed electron impact can give energy to the adsorbate and causes an electronic transition to the excited state of the adsorbate. In certain condition of the transition state, the adsorbed particles can leave the surface.

Following M. Cho (Ref. 4), we choose H$_2$O as the adsorbed species and we assume that, before the electron current begins to hit the surface, the adsorbed gas density is in a steady state. We define by $N_0$ and $W_0$ respectively the surface density and the surface energy density of desorbed neutral, volumic density is then $N_n = \frac{N_0}{W_0}$ where $d_n$ is the layer of the neutral cloud desorbed. We simply assume that the neutral cloud expands at the thermal velocity. This is given by

$$d_n = \int_0^t \sqrt{\frac{T_{surf}(x,s)}{m_n}} ds \quad (30)$$

where $T_{surf}$ is the surface temperature and $m_n$ is the neutral mass.

The surface desorption flux due to electronic impact is given by

$$\Gamma_{esd} = \frac{\partial n_e}{\partial t} = \nu_{esd} n_e \quad (31)$$

where $n_e$ is the incident electron surface density and $\nu_{esd}$ is the desorption frequency given by

$$\nu_{ESD} = \nu_0 g_{max} \frac{T_r}{T_e} \left[ 2 + \left( \frac{E_e}{T_e} + 2 \right) \exp \left( -\frac{E_e}{T_e} \right) \right] \quad (32)$$

where

- $g_{max} = \sigma_{esd} N_a$ is the maximum yield of the desorption
• \( \varepsilon_T = \varepsilon_D \cdot g_{\text{max}} D \) \((\varepsilon_D \text{ is the required desorption incident energy per neutral molecule })\)
• \( \nu_0 \) is a collision frequency with the dielectric side surface given by (ref)
• \( T_e \) is the electron temperature (eV)

Since the surface neutral flux is proportional to the incident electron surface density, we can easily calculate the neutral density over the surface by the use of a numerical scheme (see section IV) with some assumptions about the surface adsorbed neutral density \( N_a \) and the desorption cross section \( \sigma_{esd} \).

For simplicity, we assume a constant desorption cross section \( \sigma_{esd} \). The adsorbed surface neutral density \( N_a \) is renewed continuously by subtracting the number of neutral desorbed from its old value. Following M. Cho, the initial surface gas density (number of gas particles adsorbed per unit area) is assumed to be a monolayer \( N_a = 10^{19} \text{ (m}^2 \text{)} \) and the cross section is assumed to be \( \sigma_{esd} = 5 \times 10^{-19} \text{ (m}^2 \text{)} \). In this case the maximum yield \( g_{\text{max}} = \sigma_{esd} - N_a \) is five gas molecules per one incident electron (and independent of the electron incident energy if it is higher than 5 eV). The desorption yield of 5 molecules per electron corresponds to the maximum yield found in experimental studies (see Refs. 4, 5). The temperature of the desorbed gas is the same as the dielectric side surface assumed to be at \( T_{surf} = 300 \text{ (K)} \). We assume that neutral molecules do not stick back to the surface.

C. Enhanced field electron emission

In (Ref. 4) the mechanism of electron emission is EFEE (enhanced field electron emission) and the electron current density emitted is given by

\[
J = \frac{S_{FN}}{S_{\text{real}}} A(\beta E_0)^2 \exp \left(-\frac{B}{\beta E_0}\right) \text{ A/m}^2 \tag{33}
\]

which is the Fowler-Nordheim formula for field emission, with a field enhancement factor \( \beta \). Here \( A \) and \( B \) are constants determined only by the work function \( \phi_w \) of the conductor surface emission and \( E_0 \) is the electric field at the emission site. We assume that the electric field is enhanced by some mechanisms such as dielectric impurities or microscopic structures on the conductor surface (see Ref. 4 for details and references). Therefore \( S_{FN} \) is the area of the emission site on the conductor-dielectric interface and \( S_{\text{real}} \) is the area of the emission site on dielectric-vacuum interface (see figure 4).

![Figure 4: EFEE site emission](image)

IV. Numerical schemes and results

A numerical scheme was developed for the one dimensional version of the energy transport system (17) - (18) with initial and boundaries conditions and for the Poisson equation. It consists in a finite volume method. For the time integration an implicit method was developed which allows us to use long time step without facing instability problems.

The model geometry consists in a \( d = 0.1 \text{ mm} \) thickness dielectric plate with \( \varepsilon_d = 5, 5 \varepsilon_0 \) (see figure 3) where 0.1 mm is a typical thickness of a solar cell coverglass and \( \varepsilon_d = 5, 5 \varepsilon_0 \) is a typical dielectric constant of dielectric plate like \( S_t O_2 \). The conductor is biased to \(-700 \text{ V} \) while the dielectric front surface is biased to 0 V. For our geometry, it corresponds to an inverted potential gradient and the longitudinal electric field is initially \( 7 \times 10^9 \text{ (V/m)} \). We assume also an electric field of order \( 5 \times 10^6 \text{ (V/m)} \) perpendicular to the dielectric side surface leading to collisions of electrons emitted with the solid wall.

For the secondary emission we choose \( \gamma_{\text{max}} = 5, 5 \) and \( E_{\text{max}} = 500 \text{ (eV)} \) as typical value for \( S_t O_2 \).

For the field emitted electrons, we assumed cold emission, that is, the electrons are emitted with zero energy and \( T_e = 0 \text{ (eV)} \). A reasonable value for \( \phi_w \) is 4.5 eV as typical work function of a conductor. The constant \( A \) and \( B \) are given by

\[
A = 1.54 \times 10^{-10} \phi_w^{1.52}/\sqrt{\phi_w} \quad \text{ (A/m}^2 \tag{34}
\]

\[
B = 6.53 \times 10^9 \phi_w^{1.5} \quad \text{(V/m)} \tag{35}
\]

The emission site is located on the conductor and, following M. Cho (Ref. 4), we take \( S_{FN} = 10^{-15} \text{ (m}^2 \) and \( S_{\text{real}} = 10^{-11} \text{ (m}^2 \)).

Initially, we assumed that there is no plasma and no electrons confined along the dielectric surface. For the numerical resolution we choose the following initial conditions for the surface density and temperature of the electrons

\[
\left.n_e \right|_{z=0} = 0.1 \text{ (m}^{-2} \tag{36}
\]

\[
\left.T_e \right|_{z=0} = 0.1 \text{ (eV)}
\]

A. Numerical results

We show the time history of the electric field and the emission current density at the triple junction in figure 4 and figure 5.

![Figure 4: Time history of electric field at the triple junction](image)
During 1 ns the electric field is in a steady state with an initial value $E_0 = 7 \times 10^6$ (V/m); it increases rapidly after 5 ns to reach $1.6 \times 10^7$ (V/m) of magnitude at $t = 55$ ns. The current density start decreasing because of the space charge effect produced by the emission current itself. As time goes on, the EFEE emission develops rapidly because of its exponential dependence on the field $E_0$. Starting with $3 \times 10^7$ (A/m$^2$), the current density at the triple junction is $1.5 \times 10^8$ (A/m$^2$) at $t = 55$ ns.

In fact, the electrons emitted from the triple point, migrate towards the corner near $x = 0.1$ mm while acquiring energy directed in the longitudinal electric field. This leads to a reinforcement of the transverse electric field as it is shown in Figure 8.

Starting with $5 \times 10^4$ (V/m) of magnitude, it reaches to $2.5 \times 10^5$ (V/m) at the end of the simulation ($t = 55$ ns). The increase of the collision frequency at the dielectric wall results in a reinforcement of the secondary emission and the desorption.

Figure 9 shows the evolution of the density of the electrons confined along the dielectric wall. At $t = 1$ ns, the density of the electrons cloud is $7 \times 10^{16}$ (m$^{-3}$) with a maximum near the corner $x = 0.1$ mm. The avalanche seems to occur after 50 ns. Figure 10 reveals a peak where the density reaches a value of $2.5 \times 10^{18}$ (m$^{-3}$). The density profile of neutrals is exactly identical to the one of electrons. Their density reaches a value of $5 \times 10^{22}$ (m$^{-3}$) at the end of the simulation.
V. Conclusion

In this work, we have established a fluid model, more convenient for numerical simulation, for the study of dielectric discharges. An analysis of the primary discharge was developed on the idea of the discharge being driven by electric field runaway time at the triple junction, secondary emission and finally neutral desorption. The numerical simulation gives us qualitative results and shows clearly that the secondary emission play a role in the formation of a plasma cloud.

Future work will include collisions with neutral molecules in order to evaluate the probably apparition of ions.

References