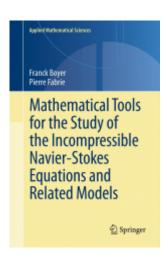
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Mathematical tools for the study of the incompressible Navier-Stokes equations and related models

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Erratum and complements

- The definition of the sound speed in the fluid on top of page 35 should be $\frac{1}{c} = \sqrt{\frac{1}{c}} T}$
- Some precisions are needed concerning Theorem VI.1.6 and Lemma VI.1.7: Details are given in this document
- In System (VI.38) the inflow part of the boundary \$\Gamma_v^-(t)\$ actually does not depend on \$t\$ since \$v=v_b\$ on the boundary and \$v_b\$ does not depend on time. However, all the analysis proposed here can be adapted to a time-dependent boundary data \$v_b\$, provided we assume suitable regularity properties.
- At the end of the statement of Theorem VI.2.1, in the case \$\inf \rho_0>0\$, it is not true that \$v\$ belongs to the space \$H\$ since its normal component does not vanish on the boundary. The correct formulation is the following \$\$v-v_b\in L^\infty(]0,T[,H)\cap N_2^{\frac{1}{4}}(]0,T[,H).\$\$

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