# Master School on Data Science and Geometry 

## INSTITUT DE MATHEMATIQUES DE TOULOUSE

2-26 july 2019

Third week PROGRAM 15-19 july

|  | Monday | Tuesday | Wednesday | Thursday | Friday |
| :--- | :--- | :--- | :--- | :--- | :--- |
| 9h00-10h30 | Optimal Transport | Statistics <br> room | MIP | MIP |  |
| $11 \mathrm{~h} 00-12 \mathrm{~h} 30$ | Optimal Transport | Statistics | MIP |  |  |
| room | MIP | MIP |  | Statistics |  |
| $14 \mathrm{~h} 00-15 \mathrm{~h} 30$ | Statistics | Optimal Transport |  | MIP |  |
| room | MIP | MIP |  | Optimal Transport | Statistics <br> MIP14h-15h00 |
| 16 h00-17h30 <br> room | Statistics | MIP |  | Optimal Transport | Optimal Transport |

## Lectures of the week

## GEOMETRY (10h) : Wasserstein geometry and optimal transport

Max FAHTI

Lecture 1 Introduction to the optimal transport problem on Euclidean space. Formulations of Monge and Kantorovitch, history, applications. Explicit solution in dimension one. Existence of solutions to the Kantorovitch problem.

Lecture 2 Kantorovitch duality, existence of a transport map solving the Monge problem. Connection with the Monge-Ampere PDE. Extension to Riemannian manifolds.

Lecture 3 Transport cost as a distance on the space of probability measures, and applications in statistics.
Lecture 4 The geometry of optimal transport: Benamou-Brenier formula and Riemannian structure of the space of probability measures. Application: gradient flow structure of the heat equation.

Lecture 5 Long-time behavior of stochastic processes, and applications to numerical schemes.

## STATISTICS (10h): Information Geometry

## Alice LE BRIGANT

Lecture 1 Statistical models, parametric estimation, sufficient statistics.
Lecture 2 Fisher information, Kullback-Leibler divergence, search for the best estimator.
Lecture 3 Fisher geometry of parametric statistical models, Fisher vs Wasserstein geometry of univariate Gaussian distributions, computing barycenters of probability distributions.

Lecture 4 Dual connections, dual geometry of exponential families, divergences.
Lecture 5 Dual connections, dual geometry of exponential families, divergences.

References: Shun-ichi Amari and Hiroshi Nagaoka, Methods of Information Geometry, American Mathematical Society, 2007.

