## Statistical Models for Road Traffic Forecasting

Mediamobile & Insitut Mathématique de Toulouse

Collaboration with: Guillaume Allain, Thibault Espinasse, Fabrice Gamboa, Philippe Goudal, Jean-Michel Loubes

17 November 2015







## Mediamobile & V-Traffic Services

Premium Traffic Information

# Mediamobile

European Leader in Traffic Broadcast



- Specialists in Traffic and Mobility since 1996
- Experts in RDS-TMC, DAB-TPEG and connected services
- Part of the TDF group, European Leader in Terrestrial Broadcast
- Present in France, Germany, Finland, Sweden, Norway, Denmark, and Poland
- Our mobility solutions are called











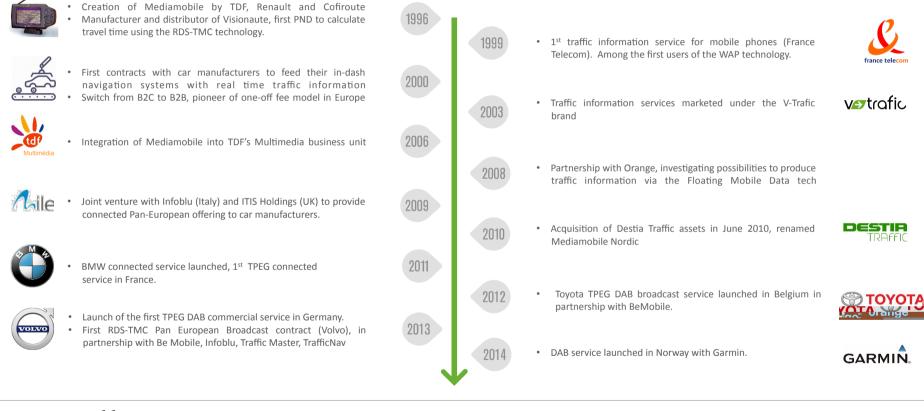
« Increase the road efficiency and the motorist safety in providing the best real time traffic and mobility information in Europe »







# V-Traffic – Key dates







# Automotive manufacturers



Confidential

5

# Navigation solutions providers

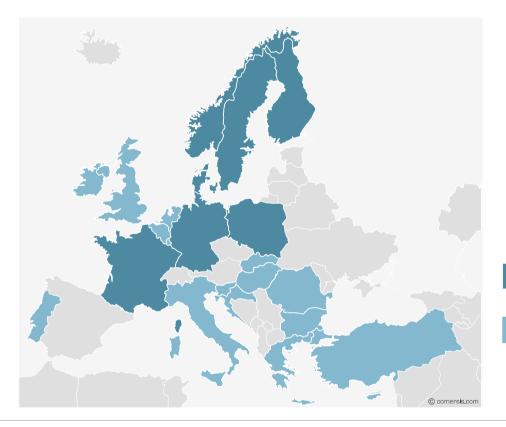






# Mediamobile & partners

Traffic services available today (all technologies)



Mediamobile offers traffic information in over 20 European countries directly, through our partner network including *BeMobile, Infoblu Trafficmaster* and *TrafficNav* ...

Mediamobile

Trafficmaster, Bemobile, InfoBlue TrafficNav

Mediamobile France Germany Sweden Finland Norway Poland Denmark Trafficmaster UK Infoblu Italy **Be-mobile** Belgium Greece Luxembourg Portugal Romania Netherlands Turkey TrafficNav Bulgaria Croatia Hungary Ireland Slovakia Slovenia





# V-traffic – mastering the value chain







## Floating Car Data Some numbers (France)

France :

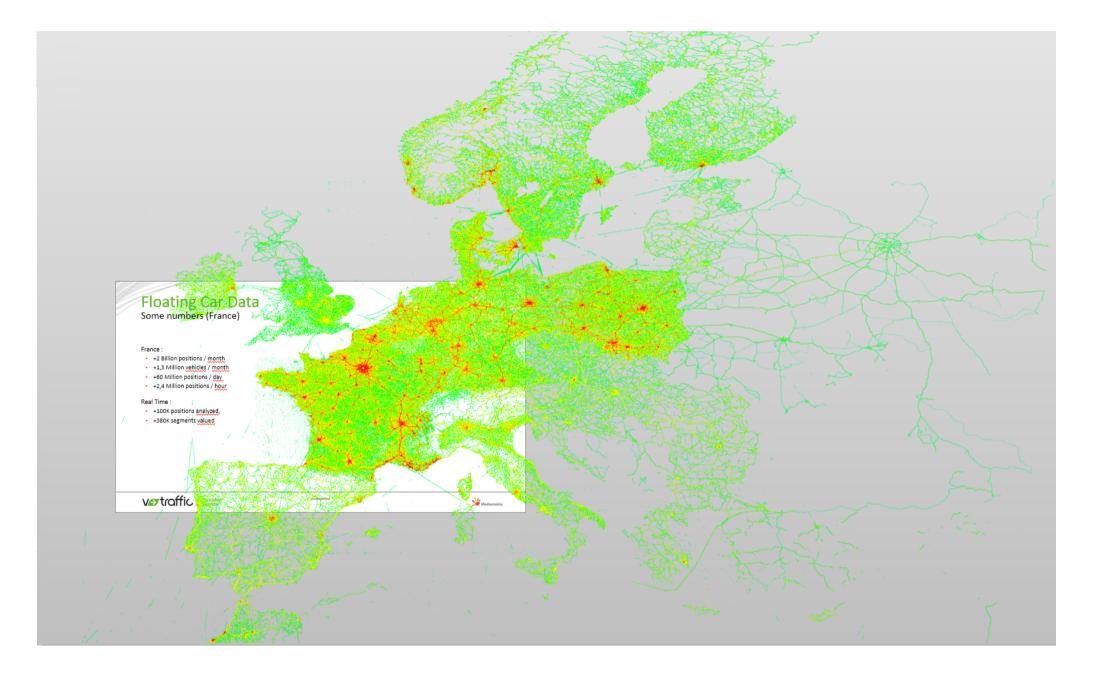
- +2 Billion positions / month
- +1,3 Million vehicles / month
- +60 Million positions / day
- +2,4 Million positions / hour

## Real Time :

- +100K positions analyzed,
- +380K segments valued

## vertraffic

Mediamobile



## Overview

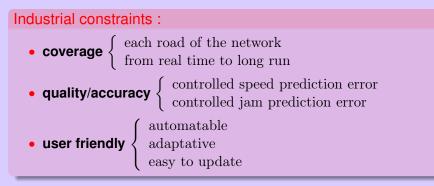
#### 1 A Big Data framework

2 Road traffic models with Machine Learning

- 3 Shape Invariant Models
- 4 Modeling velocities with Gaussian Field on a Graph

## Objectifs de l'Etude

- Gathering raw traffic information
- Processing and agregating
- Broadcasting (radio, www, mobile device...)
- $\Rightarrow$  Fancy new services : forecasting and dynamic routine



## Road traffic data-Road network

What is a road network?

- Graph composed of a set of pair (edges,vertices)
- **Complexity** of the graph  $\rightarrow$  *Functional Road Classes (FRC)*
- **FRC**  $\rightarrow$  road type classification (arterial, collector, local road...)

FRC	Number of edges	$\sum L[km]$
0	46 175	22 580
1	232 572	42 793
2	462 907	75 453
3	998 808	175 790
{0,1,2,3}	1 740 462	316 616

Tab : Number of edges by FRC

Network coverage depends on the FRC

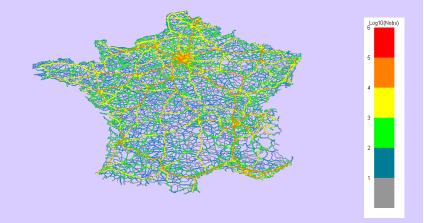
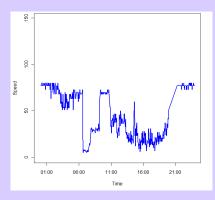


Fig : Network coverage by all FRC {0,1,2,3} from 03/01/2009 to 05/31/2009

## Speed data

What is a speed data? Loop sensor

speed calculated from flow and density (conservation law)



#### Pros

- More accurate
- 3min constant frequency

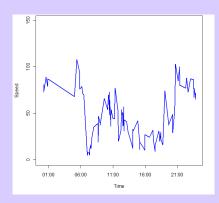
#### Cons

- Located only in main roads
- Thresholded at national speed limits

## Speed data

#### GPS sensor : Floating Car Data

• positions are mapped on a graph  $\rightarrow$  building speeds



#### Pros

- Can potentially cover all the graph
- Raw source of data

#### Cons

- Less accurate  $\rightarrow$  GPS and map-matching error
- More variable → outlier emergence
- Random frequency  $\rightarrow$  user feedback

## Observations : a big data framework

$$(x,t)\mapsto \begin{cases} & V(x,t)\\ & Y(x,t) \end{cases}$$

- V : Field of vehicle speeds observed at random time and space locations, observed partially on edges x of a graph (roads of the network) and observed when time goes by t → V(x, t).
- spatio-temporal correlations (physics of traffic) and rupture of stationnarity
- Y : variables such as traffic events, weather conditions

large scale, online data

## Overview

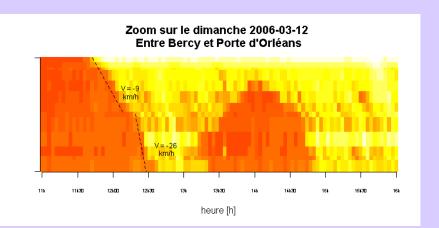
#### 1 A Big Data framework

#### 2 Road traffic models with Machine Learning

#### 3 Shape Invariant Models

#### 4 Modeling velocities with Gaussian Field on a Graph

## Local stationnarity enables to learn



## Learning Features of the road traffic

Our Goal

Appoach the road traffic dynamic with local statistical models

$$V(x_q, t_{p+h}) = \Phi(V(x, t), Y(x, t)) \rightarrow V_{q, p+h} = \Phi_{q, p, h}(\underbrace{\{V_{i,k}; i \in G, k \in T\}}_X)$$

#### Problems

- High dimension of X
- All V<sub>i,k</sub> not influent

#### Solution

- Dimension Reduction
- Promoting sparse representations
- Using methodologies
  from machine learning

Modeling traffic dynamic with significative effects only

Sparse local regression in high dimension

$$V_{q,p+h} = \Phi_{q,p,h}(V_{i,k}) \rightarrow V_{q,p+h} = \sum_{i \in G, k \in T} \beta_{i,k} V_{i,k}$$

Estimation 
$$\widehat{\beta_{i,k}} = \underbrace{K((i,k),(q,p+h))}_{Kernel}$$

Kernel selection : fit road traffic dynamic

learning a sparse set of influent parameters

$$\widehat{\boldsymbol{\beta}} = \underset{\boldsymbol{\beta}}{\text{arg\,min}} \left( \| \boldsymbol{V}_{\boldsymbol{q},\boldsymbol{p}+\boldsymbol{h}} - \sum_{i \in \boldsymbol{G}, k \in \boldsymbol{T}} \boldsymbol{\beta}_{i,k}.\boldsymbol{V}_{i,k} \|^2 + \lambda \sum |\boldsymbol{\beta}_{i,k}| \right)$$

## **Functional Clustering**

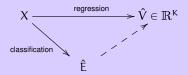
#### **Dimension reduction using Functional mixture model**

speed curve V is represented with m finite number of patterns

$$\begin{split} f_1, \dots, f_i, \dots, f_m & \text{avec } f_i \in \mathbb{R}^K \\ V = \sum_{i=1}^m \mathbbm{1}_{E=i} \ f_i + \varepsilon_i & \text{et } f^\star = f_E \end{split}$$

 $\begin{array}{l} E \in \{1, \ldots, m\} \, i.i.d. \, \text{hidden R.V.} \\ \varepsilon_i \in \mathbb{R}^K \, , \, \varepsilon_i \sim \mathcal{N}(0, \Sigma_i \in \mathcal{M}_{K,K}) \end{array} \right\} \ \mathbb{E}[V|E=i] = f_i \, , \, \text{Var}[V|E=i] = \Sigma_i \end{array}$ 

• **Classification** of E then prediction of V by  $f^*$ :

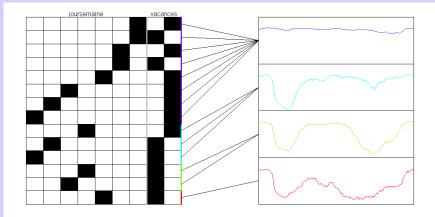


## The clustering methodology

Several ways to cluster functional data :

- Using latent variables : time, days, weather conditions
- Learning locally the active sets of variables using l<sup>1</sup> penalty or (separate or group LASSO)
- Using clustering algorithms such as k-means, kernel k-means, DBSCAN ...
- Using a better representation of the data using low rank decomposition (NMF : non negative matrix factorization) or tensor factorization

## An example of clustering model



## Allocation Rules [Patent IMT Mediamobile]

#### Frame :

- $\rightarrow$  Prediction in the day D
- $\rightarrow$  Speeds  $V^p$  are known

$$p \text{ fixed, } X = (V^p, C)$$

#### X Time series

- How many patterns ?
  - h big et p small :
    - $\Rightarrow m \text{ small}$
  - $\rightarrow~h$  small and p big :
    - $\Rightarrow \mathfrak{m} \text{ big }$
- Need for efficient clustering algorithm but off-line to get a collection of identifiable features

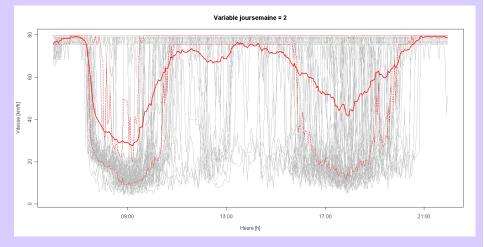
Key point : finding features that respects the structure of road trafficking .

## Overview

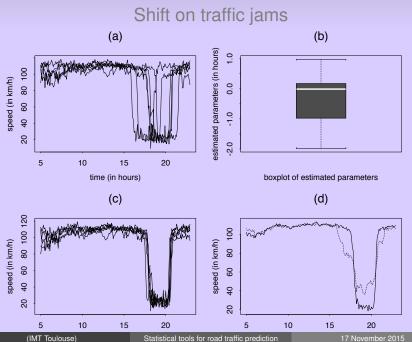
- 1 A Big Data framework
- 2 Road traffic models with Machine Learning
- 3 Shape Invariant Models
- 4 Modeling velocities with Gaussian Field on a Graph

Shape Invariant Models

## Shift on traffic jams



(IMT Toulouse)



## Registration of Shape invariant model (SIM)

From a practical question to a theoretical model : **how to extract a feature from curves with deformations** ?

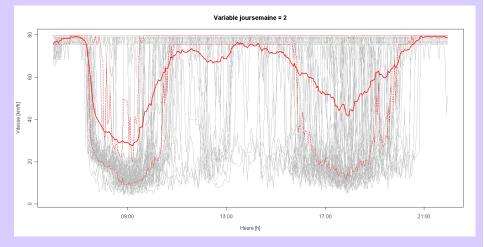
$$Y_{ij} = f_j^*(x_i) + \varepsilon_{ij} \quad i = 1...n_j, \ j = 1...J.$$

• there exists  $f^\star : \mathbb{R} \to \mathbb{R}$  with

 $f_j^*(\cdot)=a_j^*f^\star(\cdot-\theta_j^*)+\upsilon_j^*\quad (\theta_j^*,a_j^*,\upsilon_j^*)\!\in\!\mathbb{R}^3,\;\forall j=1\ldots J.$ 

f\* is the **feature** that conveys the structure of traffic data. More than 12 research papers, 4 Phd inspired by the paper by Gamboa, Loubes, Maza [2007] with several distances, online methods and other modifications Shape Invariant Models

## Shift on traffic jams

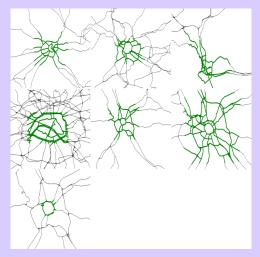


(IMT Toulouse)

## Overview

- 1 A Big Data framework
- 2 Road traffic models with Machine Learning
- 3 Shape Invariant Models
- 4 Modeling velocities with Gaussian Field on a Graph

# $\label{eq:graph} \begin{array}{c} \mbox{Graph of roads network} \\ \mbox{Modeling}: \mbox{Random process} \ (X^{(n)}_i)_{n \in \mathbb{Z}, i \in G} \end{array}$



## $\underbrace{\text{Modeling}}_{i}: \text{Random process}\; (X_i^{(n)})_{n \in \mathbb{Z}, i \in G}$

• Indexed by (discrete) time  $\mathbb Z$  and the  $\mbox{graph}\ G$  of the road traffic network

## $\begin{array}{l} Graph \ of \ roads \ network \\ \hline Modeling: Random \ process \ (X_i^{(n)})_{n\in \mathbb{Z}, i\in G} \end{array}$

• Indexed by (discrete) time  $\mathbb Z$  and the  $\mbox{graph}\ G$  of the road traffic network

Objective

Use spatial information to predict : build a model for covariance operators of X indexed by a graph

## Gaussian Process on Graph : Origin of the Problem

Trafic : Predict the speed of the vehicles with missing values

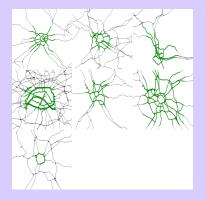
Until now : Spatial dependency is not well exploited

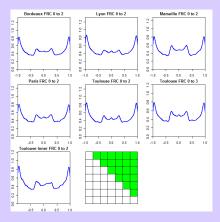
#### Aims

- Give a model that uses spatial dependency
- Estimate the spatial correlation
- Spatial filtering

Methodology : use the **spectral representation of the graph** eigenvalues and eigenvectors of the graph. The covariance of the process is a function of the spectrum of the graph.

## Spectrum of the road network

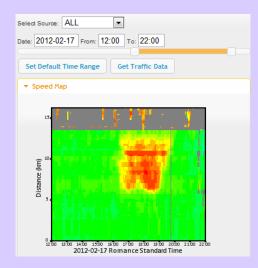




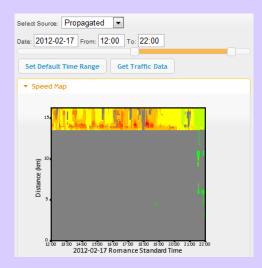
## The concrete problem



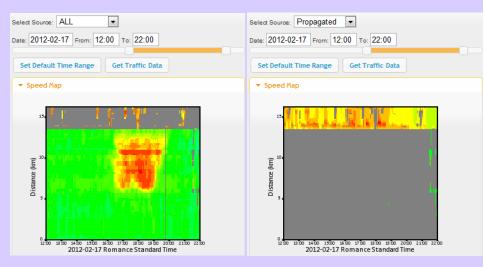
#### The concrete problem

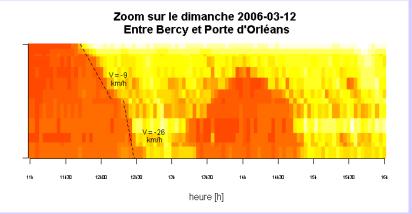


## A solution?



### Let's compare





## Thank you for your Attention



